

## Angular Separation

The angular separation between any two points on the celestial sphere is given by the following equation:

$$\theta = \left( \frac{180^\circ}{\pi} \right) \tan^{-1} \left( \frac{\sqrt{\cos^2 \delta_2 \sin^2 (\alpha_2 - \alpha_1) + [\cos \delta_1 \sin \delta_2 - \sin \delta_1 \cos \delta_2 \cos (\alpha_2 - \alpha_1)]^2}}{\sin \delta_1 \sin \delta_2 + \cos \delta_1 \cos \delta_2 \cos (\alpha_2 - \alpha_1)} \right)$$

where  $\theta$  = the angular separation between two points in decimal degrees  
 $\tan^{-1}$  = the arctangent function; if using a calculator, *be sure* it is in radians mode when you have it evaluate the arctangent function; if the arctangent is negative, add  $180^\circ$  to  $\theta$   
 $\alpha_1$  = the right ascension of the 1st point in radians  
 $\alpha_2$  = the right ascension of the 2nd point in radians  
 $\delta_1$  = the declination of the 1st point in radians  
 $\delta_2$  = the declination of the 2nd point in radians

A radian is a unit of angular measurement, and is equal to  $57.3^\circ$ . There are  $2\pi$  radians in a circle, so  $2\pi = 360^\circ$ .

You'll notice that the equation we use to find the angular separation between two points on the

<b>Greek to Me</b>	
$\theta$ = theta	$\alpha$ = alpha
$\pi$ = pi	$\delta$ = delta

celestial sphere is almost identical to the equation we use to find the shortest distance between two points on the surface of the Earth (see *Distance and Bearing*). The planet radius term  $r_p$  becomes unity (i.e. 1) for the celestial sphere, so distances become angles and we can eliminate that term from the equation. Also, we substitute right ascension ( $\alpha$ ) for its terrestrial analogue longitude ( $\lambda$ ), and likewise declination ( $\delta$ ) for its analogue latitude ( $\varphi$ ). That's all there is to it!

Let's work an example. It is commonly stated that the angular distance between the pointer stars of the Big Dipper, Merak and Dubhe (pronounced ME-rack and DUB-ee), is  $5^\circ$ . Let's use our equation to see how accurate that statement is.

Merak     $\alpha_1 = 11^{\text{h}} 01^{\text{m}} 50^{\text{s}} = 11^{\text{h}}.0306 = 165.458^\circ = 2.88779$  radians  
 $\delta_1 = +56^\circ 22' 57'' = 56.3825^\circ = 0.984060$  radians

Dubhe     $\alpha_2 = 11^{\text{h}} 03^{\text{m}} 44^{\text{s}} = 11^{\text{h}}.0622 = 165.933^\circ = 2.89608$  radians  
 $\delta_2 = +61^\circ 45' 04'' = 61.7511^\circ = 1.07776$  radians

Calculating it out, we get  $\theta = 5.37413^\circ = 5^\circ 22' 27''$ . Not bad!

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